

$$I_{NA} = \int y^2 dA$$

$$dA = t \cdot dh$$

$$y = h \cdot \sin \theta$$

$$I_{NA/2} = \int_0^{h/2} (h \cdot \sin \theta)^2 \cdot t \cdot dh$$

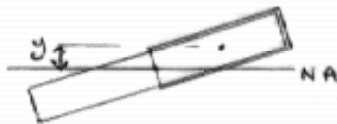
$$I_{NA/2} = \int_0^{h/2} [\sin^2 \theta \cdot h^3 \cdot t / 3]$$

$$I_{NA/2} = \sin^2 \theta \cdot l^3 \cdot t / 24$$

$$I_{NA} = \frac{\sin^2 \theta \cdot l^3 \cdot t}{12} + \frac{\cos^2 \theta \cdot l \cdot t^3}{12}$$

minor axis contrib.

PLASTIC



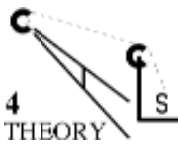
Area above NA = $l \cdot t / 2$

$y = l \cdot \sin \theta / 4$

Force = $f_c \cdot l \cdot t / 2$

Moment = $\frac{f_c \cdot l \cdot t \cdot l \cdot \sin \theta}{2 \cdot 4}$

Total Moment, $M_p = \frac{f_c \cdot l^2 \cdot t \cdot \sin \theta}{4}$



Principal and MOMENTS.

Ref. Duncan: page 260 .

I_1 is rotated θ_{12} from I_z
 I_2 " " " " I_y .

$$\begin{aligned} r - p_1 &= p_t \tan \theta & \text{--- (1)} \\ r - p_2 &= p_t \cot \theta . \end{aligned}$$

Where r = principal stress σ_1 or σ_2
 p_1, p_2 = stresses parallel to z & y axes .
 p_t = shear stress .

Assume

$$\begin{aligned} I_1, I_2 &\equiv r \\ I_z, I_y &\equiv p_1, p_2 \\ H_{zy} &\equiv p_t \end{aligned}$$

substituting in eqn (1) gives,

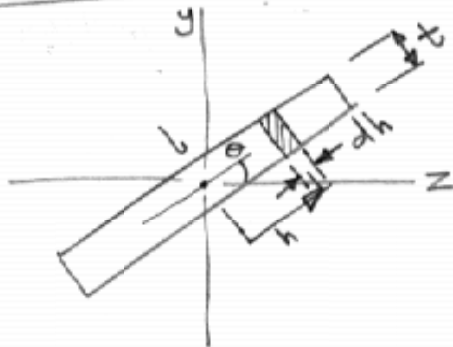
$$I_{1,2} - I_z = H_{zy} \cdot \tan \theta_{12} \quad \text{--- (2)}$$

Program Lines: -

$$\theta_{1,2} = \theta_{12} \quad \text{or} \quad \theta_{12} + \frac{\pi}{2}$$

$$I_{1,2} = -H_{zy} * \text{TAN}(\theta) + I_z$$

Product Moment of Area

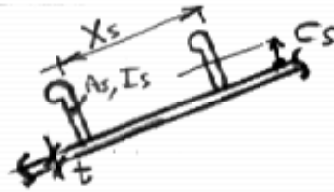


$$\begin{aligned}
 H_{zy} &= \int_{-l/2}^{l/2} z \cdot y \cdot dA \\
 &= \int \sin\theta \cdot h \cdot \cos\theta \cdot h \cdot t \cdot dh \\
 &= \left[\sin\theta \cdot \cos\theta \cdot \left(\frac{h^3}{3}\right) \cdot t \right]_{-l/2}^{l/2} \\
 &= \left(\frac{\sin\theta \cdot \cos\theta \cdot t}{3}\right) \cdot \left(\frac{l^3}{8} - -\frac{l^3}{8}\right) \\
 &= \frac{\sin\theta \cdot \cos\theta \cdot t \cdot l^3}{12}
 \end{aligned}$$

Including minor axis contribution,

$$\begin{aligned}
 H_{zy} &= \frac{\sin\theta \cdot \cos\theta}{12} (t \cdot l^3 + t^3 \cdot l) \\
 &= \frac{t \cdot l \cdot \sin\theta \cdot \cos\theta}{12} (l^2 + t^2)
 \end{aligned}$$

SSO1, bas008 mod



008.4

Input Data:

No.	Item.	x_1	y_1	x_2	y_2	t	N_s	A_s	I_s	C_s
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Calculation

No.	L	$A_p + N_s \cdot A_s$	y_p	y_s	$A \cdot y$	$A \cdot y^2$	I_o	$A_s \cdot y_o^2$
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where $y_s = y_p + C_s \cdot (x_2 - x_1) / L$ 562

$A \cdot y = A_p \cdot y_p + N_s \cdot A_s \cdot y_s$ 580

$A \cdot y^2 = A_p \cdot y_p^2 + N_s \cdot A_s \cdot y_s^2$ 590

$I_o = ((y_2 - y_1) / L)^2 \cdot (t \cdot L^3 / 12) + ((x_2 - x_1) / L)^2 \cdot N_s \cdot I_s + A_s \cdot y_o^2$ 600

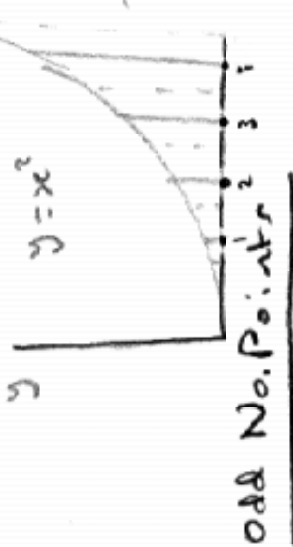
and for even no. stiffeners,

$A_s \cdot y_o^2 = ((y_2 - y_1) / L)^2 \times 2 \times A_s \cdot (L / (N_s + 1))^2 \cdot ((N_s / 2)^3 / 3)$ 6565

and for odd no. stiffeners,

$A_s \cdot y_o^2 = ((y_2 - y_1) / L)^2 \times 2 \times A_s \cdot (L / (N_s + 1))^2 \cdot (((N_s - 1) / 2)^3 / 3 + ((N_s - 1) / 2)^2 / 2 + ((N_s - 1) / 2) / 4)$ 6566

Bas008



Stiffener Contribution

odd No. Points

$$y = (x + .5)^2$$

$$= x^2 + 2 \times .5 \times x + .5^2$$

$$= x^2 + x + .25$$

$$\Phi = x^3/3 + x^2/2 + x/4 \quad \text{--- (1) } (x=0, y=0)$$

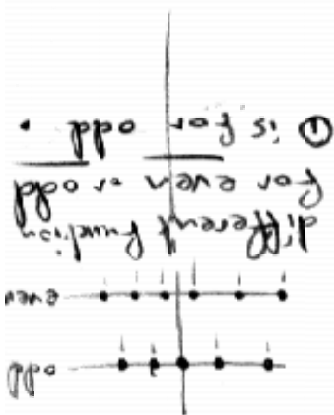
x	1	2	3	4	5	6	7	8
Φ	1.083	5.167	14.25	30.33	55.42	91.5	140.58	204.67
$\Sigma \Phi$	1.	5.	14.	30.	55.	91.	140.	204.

Even No. Points

$$y = x^2$$

$$\Phi = x^3/3 \quad \text{--- (2)}$$

x	1	2	3	4	5	6	7	8
Φ	.28	2.67	9.	21.33	41.67	72.	114.33	170.67
$\Sigma \Phi$.25	2.5	8.75	21.	41.25	71.5	113.75	170.



error reducing \rightarrow

error reducing \rightarrow

$$X_s = L / (N_s + 1)$$

$$I_y = 2 \cdot A_s \cdot \sum (i \cdot X_s)^2$$

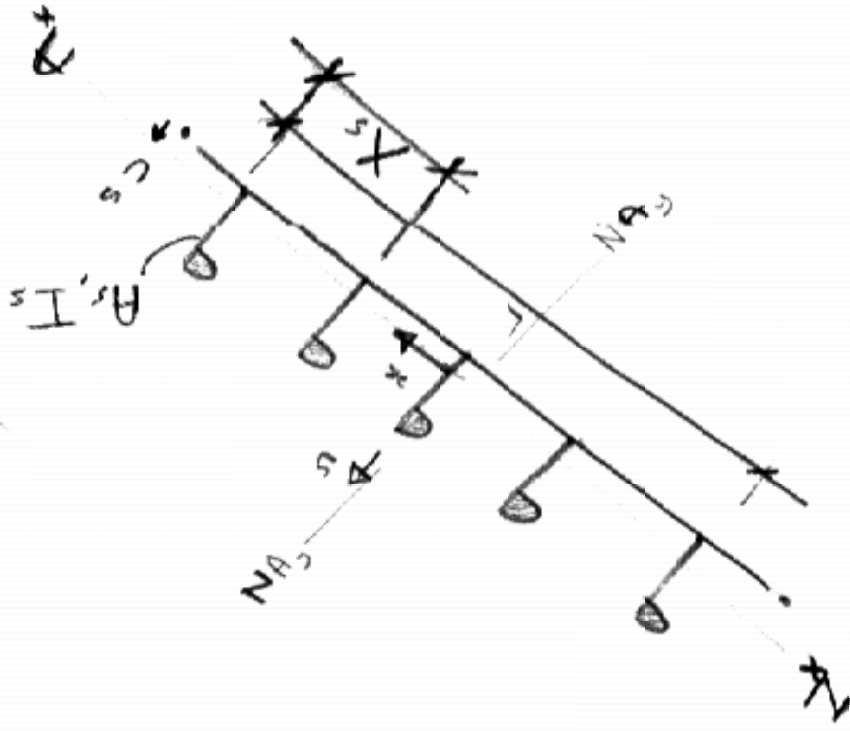
$$= 2 \cdot A_s \cdot X_s^2 \cdot \sum (i^2) \quad \text{--- (3)}$$

Odd, Sum from 1 to $(N_s - 1) / 2$

Even, Sum from 1 to $N_s / 2$

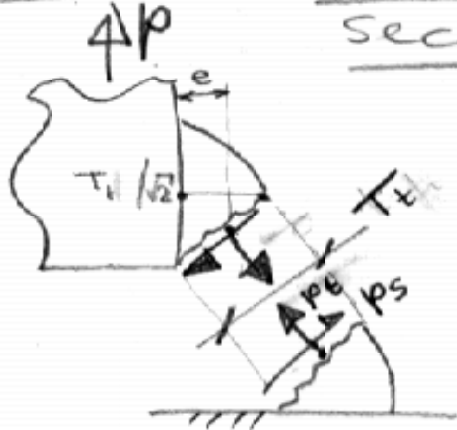
N_s , no. stiffeners on panel

009,6



Bas 008

Strength of Fillet Welded sections



Allow mix of Fillet FW & Full Pen FP to obtain total section.

Line force parts on weld, P.

Direct & Shear line forces in weld,

$$p_s = p_t = P\sqrt{2}/2$$

Stress thru weld throat,

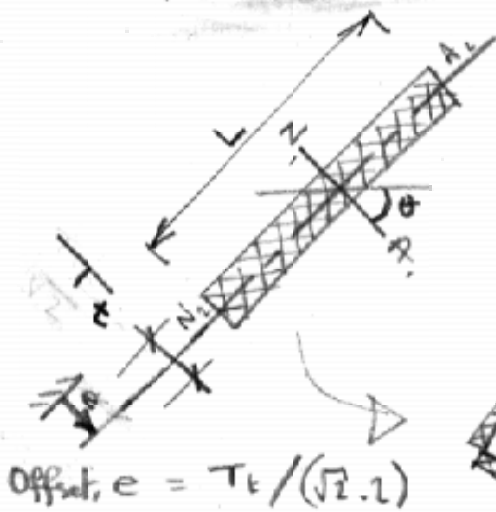
$$\sigma_s = \sigma_t = P/(\sqrt{2} \cdot T_t)$$

Then allowable shear stress, $F_d/\sqrt{3}$.

Equiv. Weld Stress,

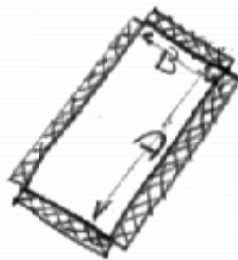
$$p_e = \sqrt{P_d^2 + 3(\gamma_{\perp}^2 + \gamma_{\parallel}^2)}$$

Fillet Weld Section Props,

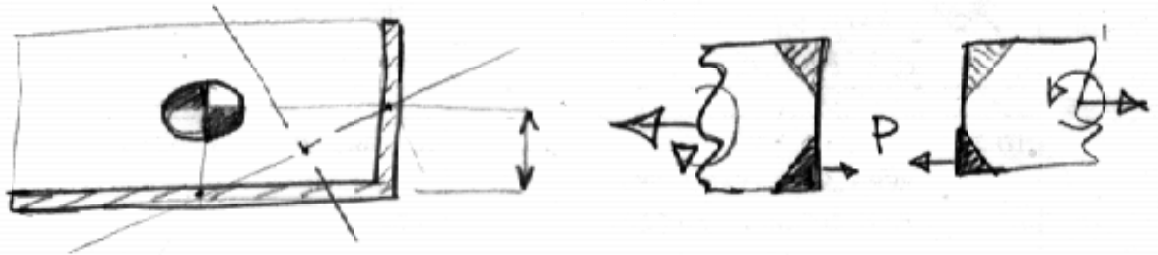


$$I_h = \frac{T_t \cdot L}{12} (T_t \cdot \sin^2 \theta + L \cdot \cos^2 \theta)$$

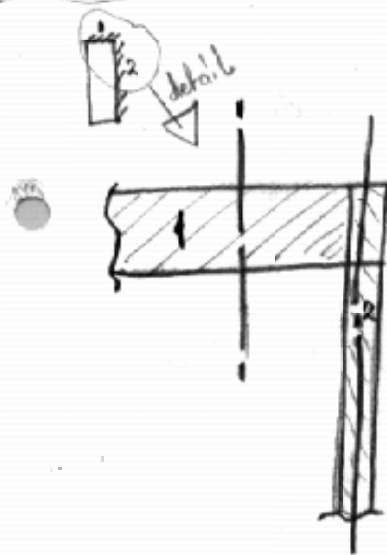
$$I_v = \frac{T_t \cdot L}{12} (T_t \cdot \cos^2 \theta + L \cdot \sin^2 \theta)$$



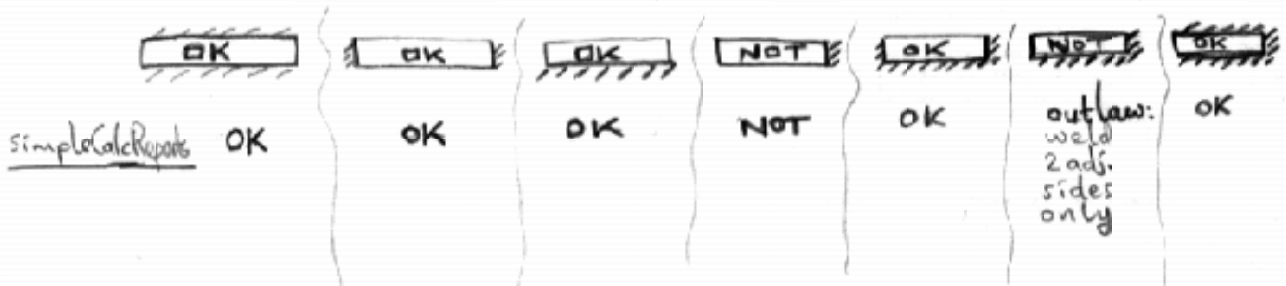
Offset, $e = T_t / (\sqrt{2} \cdot 1)$

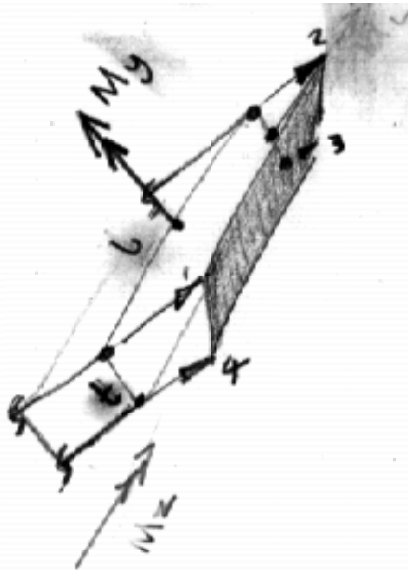


- Two or more sided welds can be balanced
- Single Cannot ... other than by putting BM thru weld
- this is only easy soln.
- Not too bad idealisation as it discriminates heavily against single sided welds



Distribute moment between adjacent sides (two welds 'L') according to rel. stiffness I_1/I_2



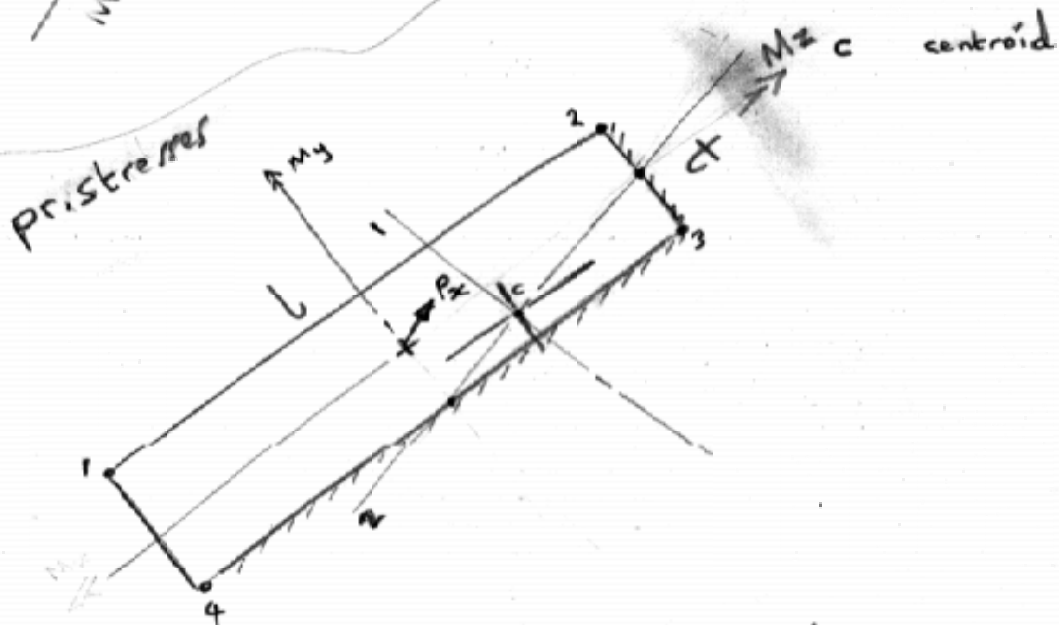


$$P_{ave} = (\sigma_1 + \sigma_2 + \sigma_3 + \sigma_4) L(b/4t) \quad (1)$$

$$\sigma = M (6 / (b d^2)) \quad \text{then,}$$

$$M_x = -((\sigma_1 - \sigma_4) + (\sigma_2 - \sigma_3)) (L t^2 / (4 \times 6)) \quad (2)$$

$$M_y = ((\sigma_1 - \sigma_2) + (\sigma_4 - \sigma_3)) (t L^2 / (4 \times 6)) \quad (3)$$



- Not quite so good as it does not simulate the general continuity of stress thru the total cross-section, although it is good for element in isolation. In this sense not worth pursuing pr. plane analysis for elements.